

Real Zeros? Number of turning points? Least Degree?

$+x^3$

$+x^4$

$+x^6$

$+x^3$

Warm Up

Oct 15-9:19 AM

KEY CONCEPT
For Your Notebook

Turning Points of Polynomial Functions

1. The graph of every polynomial function of degree n has *at most* $n - 1$ turning points.
2. If a polynomial function has n distinct real zeros, then its graph has *exactly* $n - 1$ turning points.

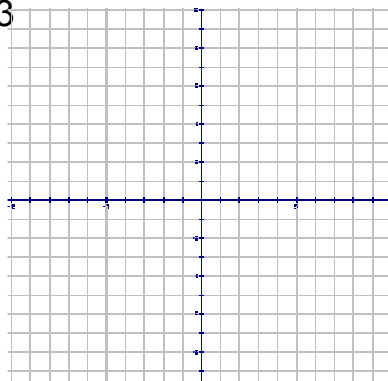
*Let's talk about the schedule!

Oct 15-10:22 AM

Graphing Higher Order Polynomials in Standard Form.

- 1) If you can't factor,
Plot points (-2, -1, 0, 1, 2)
- 2) Use general shape
- 3) Remember end behavior (consider extreme $f(-100)$, $f(100)$)

ex: $f(x) = -x^3 + x^2 + 3x - 3$

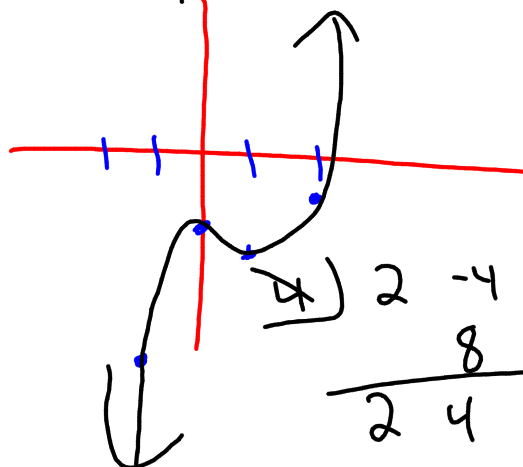


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$f(x) = 2x^3 - 4x^2 + x - 4$

x	y
-2	-38
-1	-11
0	-4
1	-5
2	-2

$\frac{4}{2} : \frac{1 \quad 2 \quad 4}{1 \quad 2}$ ± 1, 1/2, 2, 4



$\begin{array}{r} 2 \quad -4 \quad 1 \quad -4 \\ 8 \quad 16 \\ \hline 2 \quad 4 \quad 17 \quad \times \end{array}$

Oct 26-11:29 AM

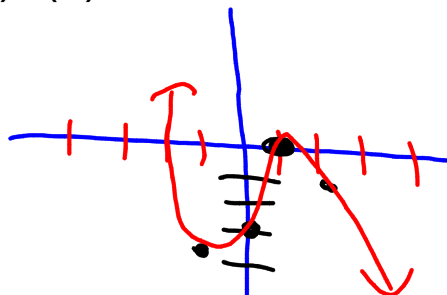
Graph the following. Label at least 3 points, including y intercepts, and describe end behavior.

1) $f(x) = 2x^3 + 8x^2 - 3$

3) $f(x) = x^4 - x^3 - 4x^2 + 4$

2) $f(x) = -x^4 - 3x^2 + x$

4) $f(x) = (-x^3 + x^2 + 3x - 3)$



$$-x^2(x-1) + 3(x-1)$$

$$(-x^2 + 3)(x-1)$$

x	y
-1	-4
0	-3
1	0
2	-1

***Pick 2!**

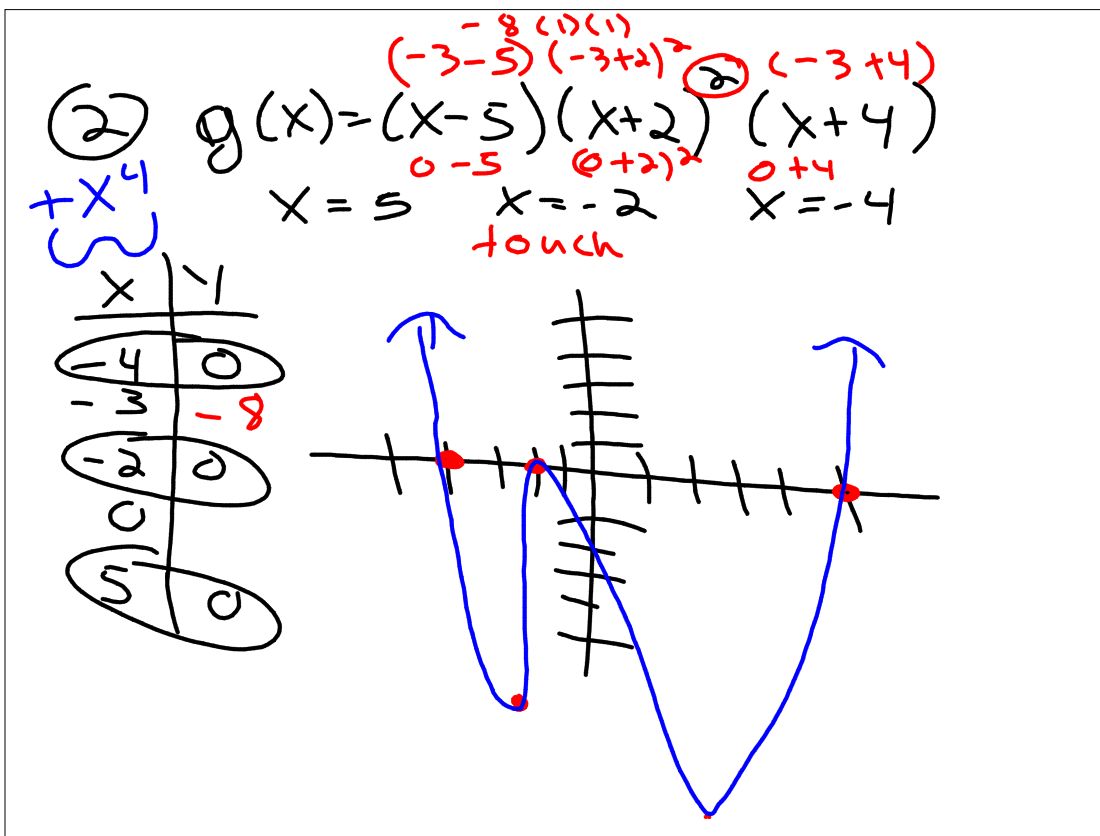
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Graphing Higher Order Polynomials in Intercept Form.

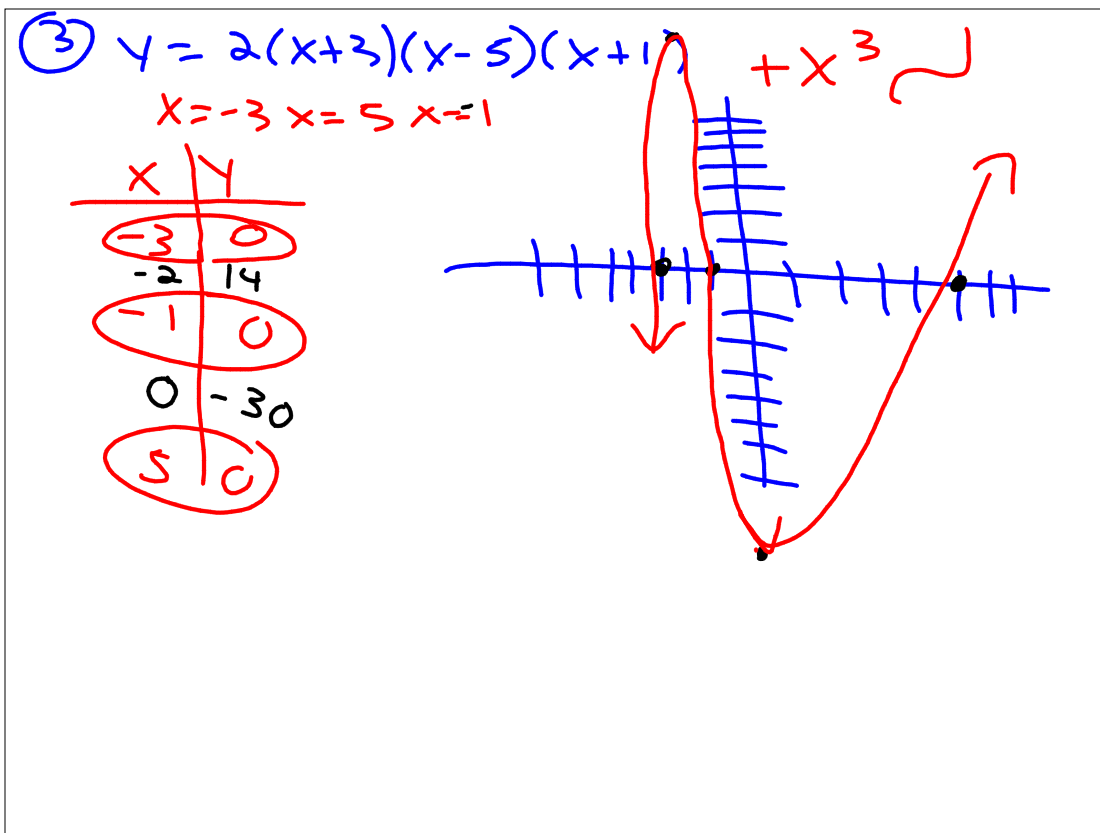
- 1) Plot intercepts as points
- 2) Plot a couple of other points in between intercepts to get general shape
- 3) Use general shape
- 4) Remember end behavior (consider extreme $f(-100)$, $f(100)$)

Ex: $f(x) = 1/3(x-5)(x+2)(x-3)$

Oct 19-9:34 PM



Oct 26-11:50 AM



Oct 26-11:55 AM

$$\textcircled{4} \quad y = (x+2)[(x+4)(x-4)]$$

$$\quad \quad \quad \downarrow \quad x^2 - 4x + 4x - 16$$

$$\quad \quad \quad (x+2)(x^2 - 16)$$

$$y = x^3 - 16x + 2x^2 - 32$$

$$y = x^3 + 2x^2 - 16x - 32$$

Oct 26-12:00 PM

$$\textcircled{5} \quad y = (x+2)(x-3)^2$$

$$y = (x+2)(x-3)(x-3)$$

$$y = (x+2)(x^2 - 6x + 9)$$

$$y = x^3 - 6x^2 + 9x + 2x^2 - 12x + 18$$

$$y = x^3 - 4x^2 - 3x + 18$$

Oct 26-12:03 PM

*Practice ws

*Vote????

Oct 25-9:34 AM

Using a function behavior to describe leading coefficient & degree of a polynomial.

*match a yellow graph with a green strip

*Let's Try one together!!!

*Work on Matching Cards

-yellow graph

-blue equation

-orange equation

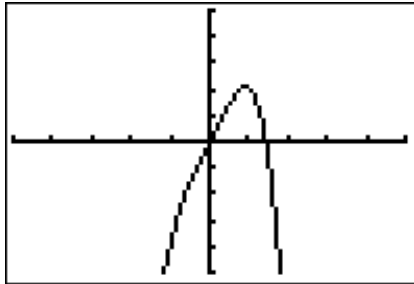
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Graphing Calculator

Real Zeros? Maximum(s)? Minimum(s)?

$$h(x) = -x^4 + 3x$$

$$g(x) = 0.5x^3 - 2x + 2.5$$



max (.91, 2.04)

zeros (0,0) (1.44, 0)



max (-1.15, 4.04) min (1.15, .96)

zero (-2.46, 0)

Oct 15-9:24 AM

Unit 3 Day 7
 Polynomial Functions
 (5.3 / 5.7) The Fundamental Theorem
 of Algebra
 and some other stuff...

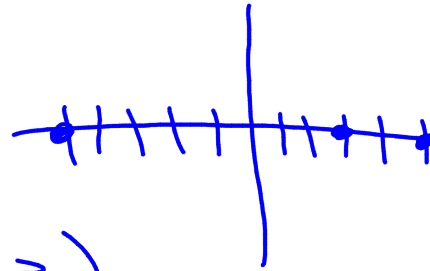
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II. FTA - Given the zeros

Find the lowest degree polynomial that has the following roots.

1.) $5, -5, 3$

$$y = (x - 5)(x + 5)(x - 3)$$



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II. FTA - Given the zeros

Find the lowest degree polynomial that has the following roots.

3.) $1, i, -i$

$$(x - 1)(x - i)(x + i)$$

$$x^2 + (x - i)(x + i)$$

$$(x - 1)(x^2 + 1)$$

$$x^3 + 1x - 1x^2 - 1$$

$$y = x^3 - x^2 + x - 1$$

$$x^2 = -1$$

$$x^2 + 1 = 0$$

$$\sqrt{x^2} = \sqrt{-1}$$

$$x = \pm i$$

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II. FTA - Given the zeros

Find the lowest degree polynomial that has the following roots.

4.) $4, -2i + 2i$

$$(x-4)(x+2i)(x-2i)$$

$$(x-4)(x^2 - 2ix + 2ix - 4i^2)$$

$$(x-4)(x^2 + 4)$$

$$y = x^3 - 4x^2 + 4x - 16$$

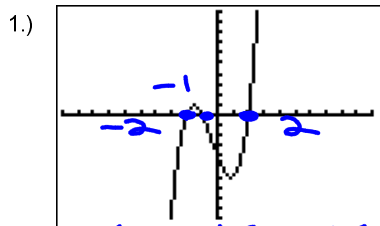
$$\sqrt{x^2} = \sqrt{-4}$$

$$x = \pm 2i$$

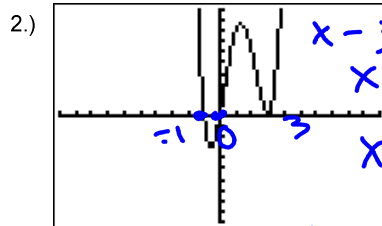
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III. FTA - Given the graph

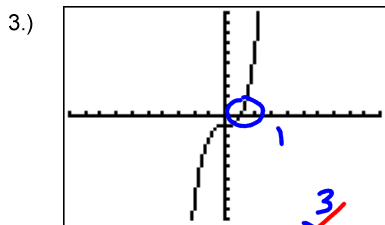
Write an equation of the polynomial.



$$f(x) = (x+2)(x+1)(x-2)$$



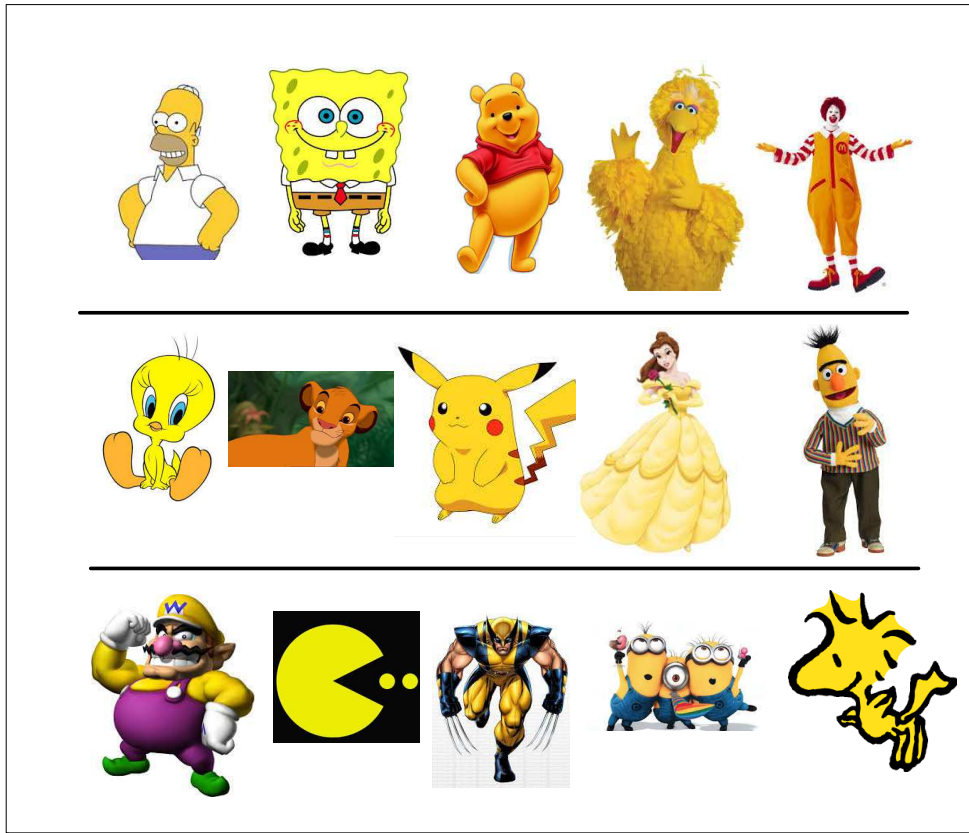
$$f(x) = x(x+1)(x-3)^2$$



$$f(x) = \cancel{(x-1)^3}$$

$$x^3 - 1$$

Oct 15-9:33 AM



Dec 30-12:22 PM

Homer Simpson	Spongebob Squarepants	Winnie the Pooh	Big Bird	Ronald McDonald
Tweety Bird	Simba	Pikachu	Belle	Bert
Wario	Pac-Man	Wolverine	The Minions	Woodstock

Dec 30-12:17 PM

IV. Polynomial Operations

Adding and Subtracting Polynomials

$$1.) \quad (\underline{2x^3} - 4x) + (\underline{-x^3} + x^2 - 2x) = x^3 + x^2 - 6x$$

$$2.) \quad (x^4 + 2x^2 - 4) - (3x^3 - 2x^2 - 2) =$$

$$x^4 - 3x^3 + 4x^2 - 2$$

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IV. Polynomial Operations

Multiplying Polynomials

$$3.) \quad -2x^2(3x^4 + x - 1) = -6x^6 - 2x^3 + 2x^2$$

$$4.) \quad (3x^2 + 1)(x - 2) =$$

$$5.) \quad (x^2 + 4)(2x^2 - x - 2)$$

$$6.) \quad (x + 4)^3 \quad (x+4)(x+4)(x+4)$$

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SPACE EXPLORATION The table shows the typical speed y (in feet per second) of a space shuttle x seconds after launch. Find a polynomial model for the data. Use the model to predict the time when the shuttle's speed reaches 4400 feet per second, at which point its booster rockets detach.

x	10	20	30	40	50	60	70	80
y	202.4	463.3	748.2	979.3	1186.3	1421.3	1795.4	2283.5

Oct 18-10:33 AM

The table shows the number of vehicles y in thousands fueled by Ethanol 85 each year x from 1999 to 2004. Find a polynomial model for the data. Use the model to predict the number of vehicles that will be fueled by Ethanol 85 in 2005.

Year	Number of Vehicles
0	24.604
1	87.570
2	100.303
3	120.951
4	133.776
5	146.195

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Homework for Friday/Monday:

Page 390/ 3, 5, 7, 8 (graphing)

Page 384/ 22-24 (writing equations)

Page 349/ 22, 34, 44, 49 (algebraic operations)

Page 398/ 25-28 (finding equation from table)

Total of 15 problems

Oct 25-9:36 AM

Word Problem WS-due on Review Day

Oct 22-9:12 AM

Homework:



CH 5 Test

-Review worksheet due next
Thursday.

Oct 7-3:19 PM